Benha University Faculty of Engineering at Shoubra Electrical Engineering Department



Electromagnetic Fundamentals Electromagnetic Fields Electrical and Electromagnetic Fields

2nd level

2024-2025

Sheet 2

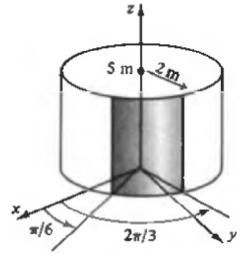
1 Determine the volume V of a region defined in a cylindrical coordinate system as $1m \le r \le 2m$, $0 \le \phi \le \frac{\pi}{3}$ rad, and $0 \le z \le 1m$ by integration. Check your result without performing the integration.

 $\left[V=\frac{\pi}{2}\ m^3\right]$

2 Determine the area S of a surface in a spherical coordinate system as r = 2 m and $\frac{\pi}{4} \le \theta \le \frac{\pi}{3}$ rad. $[A = 5.205 m^2]$

3 Use the spherical coordinate system to find the area of the strip $\alpha \le \theta \le \beta$ on the spherical shell of r = a show this strip by sketching. What result when $\alpha = 0$ and $\beta = \pi$?

- $\begin{bmatrix} A = 2\pi a^2 [\cos \alpha \cos \beta] \\ A = 4\pi a^2 \end{bmatrix}$ 4 Use the cylindrical coordinate system to find the area of the curved surface of a right
 - circular cylinder where: $r=2m\,$, $\,h=5m\,$ and $30^\circ \leq \phi \leq 120^\circ\,$ as shown in fig



 $[A = 5\pi m^2]$

Sheet 2 Page 1 of 2 5 Given the point P (5m, 60°, 2m) and Q (2m, 110°, -1m)

- (a) Find the distance $R_{\mbox{\tiny PQ}}$
- (b) Give a unit vector in Cartesian coordinates at P that is directed towards Q

$$\begin{bmatrix} R_{PQ} = 5.014 \ m \\ \overline{a}_{PQ} = -0.635\overline{a}_x - 0.489\overline{a}_y - 0.598\overline{a}_z \\ At \ point \ P \ , \overline{a}_{PQ_{cyl}} = -0.741 \ \overline{a}_{\rho} + 0.306 \ \overline{a}_{\phi} - 0.598 \ \overline{a}_z \end{bmatrix}$$

6

- (a) Find \bar{a}_x in the spherical components at *P* (3, -4,5)
- (b) Find $\bar{a}_{ heta}$ in Cartesian components at P

 $\begin{bmatrix} \overline{a}_x = \mathbf{0}.424 \ \overline{a}_r + \mathbf{0}.424 \ \overline{a}_\theta + \mathbf{0}.8 \ \overline{a}_\phi \\ \overline{a}_\theta = \mathbf{0}.424 \ \overline{a}_x - \mathbf{0}.565 \ \overline{a}_y - \mathbf{0}.707 \ \overline{a}_z \end{bmatrix}$

7 A closed surface is defined in spherical coordinates by $3 \le r \le 5$,

 $0.1\pi \leq \theta \leq 0.3\pi$, $1.2\pi \leq \phi \leq 1.6\pi$

- (a) Find the volume enclosed.
- (b) Find the total surface area.

 $\begin{bmatrix} V = 14.912 \\ Total Area = 36.8125 \end{bmatrix}$